

D. The Limit Definition

If you give your class this definition, here's one way to illustrate it with the calculator. I've never done this in a classroom so I don't know how well it works. You want to determine if

$\lim_{x \rightarrow a} f(x) = L$. Enter $f(x)$ in $y1$ and L in $y2$ and graph with

appropriate range settings. One way to get a good viewing window is to zoom in using a box around the point (a,L) .

Choose a value of ϵ and enter $L+\epsilon$ in $y3$ and $L-\epsilon$ in $y4$ and graph. Make sure that ϵ is small enough so that the lines show in your graphing window.

To determine an appropriate δ (if possible), use the **VERT** feature on the **GRAPH/DRAW** menu. Choosing **VERT** lets you position a vertical line by using the arrow keys. When the line is where you want it, press **ENTER**. Continue to use the arrow keys to position the second line and press **ENTER**. Press **GRAPH** to get out of **VERT** mode. The idea is to position the two vertical lines so that the portion of the graph of f which lies between the two vertical lines also lies between the lines $y=L\pm\epsilon$ (except possibly for the point $(a,f(a))$ if this exists). Assuming that it is possible to do this, you should now be able to determine an appropriate value of δ .

Since continuity is defined in terms of limits, there's not much new here. Jump discontinuities can be demonstrated using piecewise defined functions (Section 4).