"BRING US YOUR TIRED, YOUR POOR... TEST QUESTIONS"

Katrina B. Freeman  
Lorrie B. Joubert  
Ellen G. Stutes  
Louisiana State University at Eunice  
P.O. Box 1129  
Eunice, LA 70535  
kbroussa@lsue.edu  
lrandall@lsue.edu  
estutes@lsue.edu

Description

Software such as TI-Interactive has facilitated the creation of test questions to assess students’ higher level thinking skills. We will show some ways to incorporate this technology into the design of your college algebra assessment.

Abstract

With the growing use of graphing calculators in the classroom, there is a need for change in the methods used to assess the knowledge of the student. Until recently, the design and implementation of tests which incorporated graphing technology was difficult and time consuming. However, the development of computer programs such as TI-Interactive has made this task easier for instructors. This paper will provide examples of how this software can be used to create questions that assess higher level thinking skills rather than the age-old question of “Can they copy a graph from here to there?”
Do you find that you teach using the calculator and then test using the same old types of problems?

Graphing calculator-based problems are generally more difficult to produce and definitely more time consuming. Also, non-calculator problems typically work well for some objectives, so balancing the two types on an exam can be interesting. As graphing calculators are used more often in class to enhance learning, instructors may be inclined to include calculator problems on the quizzes and exams. This brings about the problem of creating feasible questions for assessment.

One concern of instructors who incorporate graphing calculators into the classroom is the ability of the student to understand and have a working knowledge of the calculator. In order to assess your students' knowledge, a quiz covering use of the calculator should be given early in the semester. Students should be aware of how to use the basic graphing menu, including changing the window and using the table. They should also be able to replicate basic graphs, such as a cubic function and an absolute value. At some point, students should also be made aware of the "families" of graphs so that they have an idea what the picture should look like before they look at the graph. A handout of the parent functions can easily be created using TI Interactive.

Making Connections

Using the graphing calculator to make connections between algebraic and visual learning has been one of the goals for using technology in the classroom. Students tend to make better connections if they can visualize what is occurring in a problem as well as being able to "solve" for a solution.
Examples of Connections

Finding the x-intercept(s) of a linear function or a quadratic function: When looking at a graph of an application problem, the first items we should point out are the units for the x-values and the y-values. Many students are still thinking in terms of x and y instead of real-life units. The x-intercept has more meaning for a student if they are trying to find how many products should be produced in order to break even in a profit situation. Even though we can use the polynomial solver to find these solutions, the graph gives a visual effect of where the profit is negative (a loss) and where the profit is positive (a gain). The following graph illustrates the profit function

\[ P(s) = 6.5s - 110000 \]

Another example that can be used to help make the connection between points on the graph and a real-life situation is the projectile function. The y-intercept and the x-intercept take on new meaning if they can be approached as the initial height of the object (before it is thrown or dropped) and the time at which the object hits the ground. This is also a good time to bring in domain and range. For example, does \( y = -3 \) have any meaning here? It is much easier to connect the vertex as a maximum point if the student can see this point on the graph. Of course, by using the calculator and the graphing menu (the calculate menu), the values for these points are easier to obtain than if calculated algebraically.
\[ h(t) = -16t^2 + 64t + 200 \]

Inequalities also fall into the category of making connections between algebraic problems and graphing. Many inequalities are set up to compare two plans of action. A popular question to introduce this idea concerns Bar A which has a cover charge of $5 but the beer is only $1.25 versus Bar B which has no cover charge and charges $2.50 per beer. Let \( x \) = the number of beers you drink and then \( y = \) cost to drink at that bar. After discussing which bar is better for you and your friends, the students come to the conclusion that at some point, they are equal. Solving algebraically, they find that at 4 beers, the cost is the same for both bars. Graphing the two equations on the same set of axes, we see that the point where both have the same cost is the intersection of the two lines. To introduce the idea of inequality, you can use the trace function to show the cost of 2 beers for each bar and then 5 beers for each bar. This helps them to see that if you drink less than 4 beers, Bar B is the better deal (the cost is less) and after 4 beers, the inequality is reversed and Bar A is cheaper.
Designing Test Questions

When designing test questions, you should first decide if you wish to test the students' knowledge of graphing or if you really wish to test their understanding of the graph itself and the significant ordered pairs that we find there.

TI Interactive makes it easier to create different types of assessment questions. You could create matching questions where the student matches the appropriate window to each picture. Another suggestion is to give the students the equation and then have them sketch the graphs using different window settings to find the "most complete" picture of the graph. This enables them to see that the picture changes with a change in the window settings.

If you are testing their ability to replicate a graph, then using a sketch of the coordinate system may be appropriate. Including scales on the axes will help the student to set the window accordingly on their calculator. This allows you to move away from graphing the "simple" equations that fit on the standard window to graphing any equation on an appropriate window.

For example, sketch the graph of \( f(t) = 2000e^{0.14t} \).

![Graph of \( f(t) = 2000e^{0.14t} \).](image.png)

If testing their ability to find information from a graph (application-type problems), it is more convenient to give the formula and the graph so that they can recreate the graph on their own calculators in order to use the calculate functions and the table to answer questions. For
example, if $f(t) = 2000e^{0.1t}$ models the population of a town $t$ years after 1985, the following questions could be posed:

a. Find the population in the year 2000. (The student could use the table or the trace function to answer the question).

b. When will the population reach 5000? (The student could graph the equation and $y = 5000$ then find the intersection.)

Another example of testing their ability to interpret a graph is an application involving cell phone charges. If the plan is $40 for the first 500 minutes and $5 for each additional 100 minutes used in the month, the following graph could be used.

![Graph showing cost vs. number of minutes]

**Summary**

The use of TI Interactive has made it easier to incorporate graphing calculator based questions on quizzes and test. These problems assess the students’ comprehension of an application rather than testing their ability to graph. By using the graphing calculator in the classroom and on assessments, instructors can move away from creating tables and plotting points to making visual connections which enhance comprehension.